

# Gravity Mediation in 6d Brane-World Supergravity <sup>1</sup>

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**Abstract.** We consider the gravity-mediated SUSY breaking within the effective theory of six-dimensional brane-world supergravity. We construct the supersymmetric bulk-brane action by Noether method and find the nontrivial moduli coupling of the brane F- and D-terms. We find that the low energy Kähler potential is not of sequestered form, so gravity mediation may occur at tree level. In moduli stabilization with anomaly effects included, the scalar soft mass squared can be positive at tree level and it can be comparable to the anomaly mediation.

**Keywords:** Supergravity, Orbifolds, Supersymmetry breaking, Gravity mediation.

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## INTRODUCTION AND SUMMARY

When supersymmetry(SUSY) breaking is parametrized by soft mass parameters which respect the Standard Model gauge symmetry, there would occur new dangerous CP and/or flavor violations. As a generic consequence of local SUSY, gravity mediation of hidden sector SUSY breaking generates all required soft mass terms of order the weak scale [1]. Generically, however, there appear contact terms between visible and hidden sectors in the Kähler potential as

$$\begin{aligned} \Omega = & -3M_p^2 + \Omega_0(Q_H, \bar{Q}_H) \\ & - \frac{1}{3M_p^2} \left( \delta_{ij} + C_{ij}(Q_H, \bar{Q}_H) \right) \bar{Q}_V^i Q_V^j + \cdots \end{aligned} \quad (1)$$

For a non-diagonal contact term  $C_{ij}$ , the supergravity F-term potential in the hidden sector would lead to visible soft scalar mass with  $\mathcal{O}(1)$  off-diagonal components.

In higher dimensional supergravity where extra dimensions are compactified on orbifolds, one can find a more fundamental origin of contact terms [2]. First, when the visible sector is located at the orbifold fixed point, it can be geometrically separated from the hidden sector which is located at a different fixed point. Second, while effects of heavy bulk fields to contact terms are suppressed for large extra dimensions, contact terms can be computed within the effective field theory by integrating out Kaluza-Klein modes of bulk fields. If SUSY breaking is mediated dominantly by higher dimensional gravity multiplet, it is guaranteed that generated contact terms are flavor universal.

For instance, in 5d minimal supergravity compactified on  $S^1/\mathbf{Z}_2$  [3, 4, 5, 6], sequestering of visible sector is manifest in the low energy Kähler potential ( $K = -3 \ln \Omega$ ) as

$$\Omega = \frac{1}{2}(T + \bar{T}) - \frac{1}{3}\Omega_V(Q_V, \bar{Q}_V) - \frac{1}{3}\Omega_H(Q_H, \bar{Q}_H). \quad (2)$$

Because of the no-scale structure, soft masses are zero at tree level, which is attributed to locality of SUSY breaking sector in extra dimension. Therefore, in this case, the no-scale structure of tree-level Kähler potential must be lifted by loop-corrections. The anomaly mediation is a generic consequence in the off-shell formulation of 4d supergravity [2] and it may be a dominant contribution to soft masses. Since the anomaly mediation gives a flavor-universal contribution to soft masses, it would help ameliorate the SUSY flavor problem. However, there arises a serious problem with negative slepton mass squared. Moreover, one-loop gravitational correction to the scalar soft mass squared also turned out to be negative [6, 8]. Generalizing the setup to warped supergravity does not improve the situation [7, 8]. In models with sizable brane gravity kinetic terms, however, positive scalar masses can be obtained [6, 7].

On the other hand, it has been pointed out in ref. [9] that sequestering is absent in higher dimensional brane-world supergravity. In this case, when KK modes of bulk fields are involved in the tree-level exchange between different sectors, their decoupling may lead to (generically non-diagonal) non-local contact terms at tree level which are not suppressed in comparison to the gravitino mass.

In this talk, we consider the gravity-mediated SUSY breaking in the context of 6d minimal supergravity [10, 11]. We compactify two extra dimensions on  $T^2/\mathbf{Z}_2$  and impose the orbifold boundary conditions on the component fields of supergravity multiplet. We construct the supersymmetric bulk-brane action by Noether method and

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find the nontrivial moduli coupling of the brane F- and D-terms. From the obtained low energy effective action, we find that there is no sequestering in the Kähler potential any more. Because of a tree-level coupling between the visible and hidden sectors, tree-level scalar soft masses in the visible sector may be generated. However, it crucially depends on the form of the effective superpotential. If moduli are stabilized by the brane D-term with the effective superpotential which does not depend on the  $T$  modulus, there is a sequestering in the scalar potential. On the other hand, when one takes into account the effect of anomalies, the superpotential gets a correction with the  $T$  modulus dependence. In this case, the scalar soft mass squared can be positive at tree level and it can be comparable to the anomaly mediation.

## SUPERGRAVITY ON $T^2/Z_2$

The 6d minimal supergravity multiplet is composed of graviton ( $e_M^A$ ), gravitino ( $\psi_M$ ), Kalb-Ramond field ( $B_{MN}$ ), dilaton ( $\phi$ ) and dilatino ( $\chi$ ). The 6d chirality conditions are  $\Gamma^7 \psi_M = \psi_M$  and  $\Gamma^7 \chi = -\chi$ . For the absence of 6d gravitational anomalies, one needs additional multiplets with  $n_H = 244 + n_V - n_T$  where  $n_V = \dim G$  and  $n_H(n_T)$  is the number of hyper(tensor) multiplets. However, we assume the additional multiplets get a heavy mass and they are irrelevant for SUSY breaking. In this work, we focus only on the gravity mediation of SUSY breaking.

We regard two extra dimensions to be compactified on a torus with periodicities  $z \equiv z + 2\pi(m + in\tau)R$  where  $z = x_5 + i\tau x_6$  with  $x_{5,6} \equiv x_{5,6} + 2\pi R$  and  $\tau = \tau_2 + i\tau_1$  is the complex structure. In this coordinate basis, the 2d metric is given by  $ds_2^2 = g_{mn}dx^m dx^n$  with

$$g_{mn} = -\frac{A}{\tau_2} \begin{bmatrix} 1 & \tau_1 \\ \tau_1 & \tau_1^2 + \tau_2^2 \end{bmatrix}. \quad (3)$$

Let us impose the  $Z_2$  orbifold symmetry on the torus. By identifying  $(x_5, x_6)$  with  $(-x_5, -x_6)$ , there appear four orbifold fixed points:  $(0, 0)$ ,  $(\pi R, 0)$ ,  $(0, \pi R)$ ,  $(\pi R, \pi R)$ . Decomposing the 6d spinor into 4d form as  $\Psi \equiv (\psi^1, \bar{\psi}^2)^T$ , we assign even  $Z_2$ -parity to

$$e_{\mu}^{\bar{v}}, e_{\bar{m}}^{\bar{v}}, B_{\mu\nu}, B_{mn}, \phi, \psi_{\mu}^1, \psi_{\bar{m}}^2, \chi^2, \quad (4)$$

and odd  $Z_2$ -parity to

$$e_{\mu\bar{m}}, B_{\mu\bar{m}}, \psi_{\mu}^2, \psi_{\bar{m}}^1, \chi^1. \quad (5)$$

Then, one massless  $\mathcal{N} = 1$  supergravity multiplet is built from zero modes of  $e_{\mu}^{\bar{v}}$  and  $\psi_{\mu}^1$ ; three massless  $\mathcal{N} = 1$  chiral multiplets from zero modes of  $e_{\bar{m}}^{\bar{v}}, B_{\mu\nu}, B_{mn}, \phi, \psi_{\bar{m}}^1$  and  $\chi^2$ ; and a KK tower of (short) massive multiplets of  $\mathcal{N} = 2$  supergravity and two massive  $\mathcal{N} = 1$  vector multiplets.

*Brane couplings of moduli.* A Noether construction of the bulk-brane action [12] gives a nontrivial dilaton coupling to a brane chiral multiplet as

$$\mathcal{L}_Q = e_4 \left[ e^{-\phi} D^{\mu} Q^{\dagger} D_{\mu} Q + \frac{i}{2} e^{-\phi} \bar{\Psi}_Q \gamma^{\mu} D_{\mu} \Psi_Q + \dots \right] \quad (6)$$

Moreover, the brane action of a vector multiplet gives the brane D-term with a dilaton coupling as

$$\mathcal{L}_D = -e_4 \frac{1}{2} e^{-2\phi} g^2 D^2. \quad (7)$$

In terms of  $Z_2$ -even components of gravitino, we can construct a gravitino mass term at the fixed point as

$$\begin{aligned} \mathcal{L}_W = & e_4 \frac{1}{2} \sqrt{\frac{A}{\tau_2}} W_0 (-\bar{\Psi}_{\mu} \gamma^{\mu\nu} C \bar{\Psi}_{\nu}^T + i \bar{\Psi}_{+} \gamma^{\mu} C \bar{\Psi}_{\mu}^T \\ & + i \bar{\Psi}_{-} \gamma^{\mu} C \bar{\Psi}_{\mu}^T + \text{h.c.}) \end{aligned} \quad (8)$$

where  $\Psi_{\pm} = -(\psi_5^2 \pm i\psi_6^2)$  and  $W_0$  is a constant brane superpotential. The result is generalized to a field-dependent brane superpotential  $W = W(Q)$ . Thus, we also get the brane F-term with a nontrivial moduli dependence as

$$\mathcal{L}_F = -e_4 \frac{A e^{\phi}}{\tau_2} |F|^2 \quad (9)$$

with  $F = \partial_Q W$ .

## GRAVITY MEDIATION OF SUPERSYMMETRY BREAKING

*Low energy supergravity.* We take the 6d metric as

$$ds^2 = A^{-1}(x) g_{\mu\nu}(x) dx^{\mu} dx^{\nu} + ds_2^2 \quad (10)$$

and plug the metric into the 6d action. Then, from the resulting kinetic terms of bosonic action [12], we find the Kähler potential in the 4d effective supergravity as

$$\begin{aligned} K = & -\log \left( \frac{1}{2} (T + \bar{T}) - \frac{1}{M_p^2} |Q|^2 \right) \\ & -\log \left( \frac{1}{2} (S + \bar{S}) \right) - \log \left( \frac{1}{2} (\tau + \bar{\tau}) \right) \end{aligned} \quad (11)$$

with  $M_p^2 \equiv (2\pi)^2 M_6^4$ , and

$$\begin{aligned} T &= t + \frac{1}{M_p^2} |Q|^2 + i\sqrt{2} B_{56}, \\ S &= s + i\sqrt{2} a, \quad \tau = \tau_2 + i\tau_1, \end{aligned} \quad (12)$$

where  $s = A e^{-\phi}$ ,  $t = A e^{\phi}$ , and  $e^{-2\phi} H_{\mu\nu\rho} = \epsilon_{\mu\nu\rho\sigma} \partial^{\sigma} a$ . Moreover, we find that the brane gauge kinetic function does not depend on moduli. By comparing eq. (8)

to the 4d standard formula for the gravitino mass as  $\mathcal{L}_m = -\frac{1}{2}e_4 e^{K/2} W \bar{\psi}_\mu \gamma^{\mu\nu} C \bar{\psi}_\nu^T$ , we can also see that the effective brane superpotential does not depend on moduli.

*Gravity mediation.* With the visible and hidden sectors at two different fixed points, the relevant Lagrangian in 4d superconformal frame is given by

$$\mathcal{L} = -3M_p^2 \int d^4\theta \Phi^\dagger \Phi \Omega \quad (13)$$

where  $\Phi = 1 + \theta^2 F_\Phi$  is the compensator field, and  $\Omega = e^{-K/3}$  is given by

$$\begin{aligned} \Omega &= \frac{1}{2}(T + \bar{T} - 2\Omega_V - 2\Omega_H)^{1/3} (S + \bar{S})^{1/3} (\tau + \bar{\tau})^{1/3} \\ &\simeq \frac{1}{2}(T + \bar{T})^{1/3} (S + \bar{S})^{1/3} (\tau + \bar{\tau})^{1/3} \\ &\times \left[ 1 - \frac{2}{3} \frac{\Omega_V + \Omega_H}{T + \bar{T}} - \frac{8}{9} \frac{\Omega_V \Omega_H}{(T + \bar{T})^2} \right]. \end{aligned} \quad (14)$$

As a consequence, we find that there is no sequestering of visible sector in the Kähler potential even at tree level. For general SUSY breaking including the brane D-term, scalar soft mass in the visible sector is expressed in terms of the gravitino mass  $m_{3/2}$  and F-terms as

$$\begin{aligned} m_{QV}^2 &= 4m_{3/2}^2 - 2 \frac{|F_T|^2}{(T + \bar{T})^2} - \frac{|F_S|^2}{(S + \bar{S})^2} \\ &\quad - \frac{|F_\tau|^2}{(\tau + \bar{\tau})^2} - 4 \frac{|F_H|^2}{(T + \bar{T})}, \end{aligned} \quad (15)$$

with  $F_i = -e^{K/2} (K^{-1})_{ij} D_j W$ , while a vanishing cosmological constant imposes a condition

$$\begin{aligned} \frac{2D^2}{M_p^2 (T + \bar{T})^2} &= 3m_{3/2}^2 - \frac{|F_T|^2}{(T + \bar{T})^2} - \frac{|F_S|^2}{(S + \bar{S})^2} \\ &\quad - \frac{|F_\tau|^2}{(\tau + \bar{\tau})^2} - 2 \frac{|F_H|^2}{(T + \bar{T})}. \end{aligned} \quad (16)$$

## MODULI STABILIZATION AND SOFT MASS TERMS

From the brane terms (7) and (9) with eq. (12), we obtain the effective scalar potential as

$$V = \frac{|F|^2}{[(S + \bar{S})/2][(\tau + \bar{\tau})/2]} + \frac{D^2}{[(T + \bar{T})/2 - |Q|^2]^2}. \quad (17)$$

This is of the run-away type, so there is no local minimum for moduli. Thus, in order to stabilize moduli, we need additional contributions in the scalar potential due to bulk dynamics.

*Bulk gaugino condensation.* The gauge kinetic function for zero mode of bulk vector multiplet is, at tree level,

$$f = \frac{1}{g_4^2} S \quad (18)$$

where  $g_4^2 = g_6^2 / (2\pi R)^2$  with  $g_6$  the 6d gauge coupling. When there are two gaugino condensates in the bulk below the compactification scale, the nonperturbative effective superpotential is generated to be of racetrack form [13],

$$W = (\eta(i\tau))^{-2} (\Lambda_1 e^{-c_1 S} + \Lambda_2 e^{-c_2 S}) \quad (19)$$

where  $\eta(i\tau)$  is the Dedekind eta function,  $c_1, c_2, \Lambda_1, \Lambda_2$  are constants. Here we note that the moduli invariance associated with the shape of a torus requires the  $\tau$  dependence in the superpotential.

*Stabilization of  $S$  and  $\tau$ .* In the presence of the non-perturbative superpotential, the scalar potential is minimized for  $F_S = F_\tau = 0$ . Then, the local minimum of  $S$  is

$$\text{Re} S = \frac{1}{c_1 - c_2} \log \left[ \frac{\Lambda_1 (2c_1 \text{Re} S + 1)}{\Lambda_2 (2c_2 \text{Re} S + 1)} \right], \quad (20)$$

$$\text{Im} S = \frac{\pi(2n+1)}{c_1 - c_2}, \quad n \in \mathbf{Z}, \quad (21)$$

and

$$\hat{G}_2 \equiv -2\pi \left( \partial_\tau \log \eta(i\tau) + \frac{1}{\tau + \bar{\tau}} \right) = 0, \quad (22)$$

leads to a local minimum  $\tau = \sqrt{3}/2 + i/2$  (another zero  $\tau = 1$  is a saddle point.).

*Stabilization of  $T$ .* After stabilization of  $S$  and  $\tau$ , there remains the scalar potential for  $T$  as

$$\begin{aligned} V/M_p^2 &= -\frac{2\hat{m}_{3/2}^2 - |\hat{F}_S|^2 - |\hat{F}_\tau|^2}{(T + \bar{T})} + 2|\hat{F}_H|^2 \\ &\quad + \frac{2D^2}{(T + \bar{T})^2} \end{aligned} \quad (23)$$

where  $\hat{m}_{3/2}, \hat{F}_S, \hat{F}_\tau$  and  $\hat{F}_H$  are  $T$ -independent constants proportional to the quantities without the hat. The  $T$ -modulus is stabilized with zero vacuum energy, provided that

$$\frac{2D^2}{(T + \bar{T})^2} = 2|\hat{F}_H|^2 = \frac{\hat{m}_{3/2}^2 - \frac{1}{2}|\hat{F}_S|^2 - \frac{1}{2}|\hat{F}_\tau|^2}{(T + \bar{T})}. \quad (24)$$

After stabilization of all moduli, the scalar soft mass vanishes. One-loop gravity correction to the Kähler potential

does not generate a soft mass either. The real part of  $T$ -modulus gets a mass as

$$m_T^2 = \frac{8D^2}{(T + \bar{T})^2} \simeq 4m_{3/2}^2. \quad (25)$$

The axionic part of  $T$ -modulus could be eaten up by a bulk gauge field via Green-Schwarz mechanism.

*Anomaly corrections.* Even though the 6d irreducible anomalies can be cancelled by the introduction of additional multiplets, generically one also needs a Green-Schwarz counterterm [14] to cancel the reducible part of anomalies. Then, after a supersymmetric completion of the GS term [15, 16], the bulk gauge kinetic term gets modified to

$$f_a = \frac{1}{g_a^2}(S + \alpha_a T) \quad (26)$$

where  $\alpha_a$  depends on bulk fermion content. As illustration, when there are multiple gaugino condensates with anomaly corrections, the effective superpotential can be

$$W = (\eta(i\tau))^{-2} W(S)W(T) \quad (27)$$

with

$$W(S) = \Lambda_1 e^{-c_1 S} + \Lambda_2 e^{-c_2 S}, \quad (28)$$

$$W(T) = \Lambda_3 e^{-c_3 T} + \Lambda_4 e^{-c_4 T}. \quad (29)$$

For  $F_S = F_\tau = F_T = 0$ , there exists a AdS minimum with all moduli stabilized. Then, the  $T$ -modulus mass is given by

$$m_T^2 \sim c_3^2 c_4^2 (T + \bar{T})^4 m_{3/2}^2. \quad (30)$$

For  $|c_3 - c_4| \ll c_3$ ,  $(T + \bar{T})$  can be large enough and  $m_T^2 \gg m_{3/2}^2$ .

In order to lift the vacuum up to a Minkowski vacuum, one needs a positive lifting potential such as the brane F-term and/or D-term. In this lifting procedure, SUSY is broken and a nonzero soft mass can be generated at tree level. When the D-term lifting potential is dominant as

$$\frac{D^2}{(T + \bar{T})^2} \sim m_{3/2}^2 M_P^2, \quad \frac{|F_H|^2}{(T + \bar{T})} \ll m_{3/2}^2, \quad (31)$$

the scalar soft mass squared tends to be positive. If the D-term is comparable to the F-term, tree-level soft masses can be comparable to the contribution from anomaly mediation.

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